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## ECONOMETRIC THEORY REVIEW QUESTIONS

## **Monte Carlo tests**

1. Consider the linear regression model

$$y = X\beta + u \tag{1}$$

where y is a  $T \times 1$  vector of observations on a dependent variable, X is a  $T \times k$  fixed matrix of explanatory variables (observed),  $\beta = (\beta_1, \ldots, \beta_k)'$ , and u is a  $T \times 1$  vector of unobserved error terms.

- (a) Suppose the elements of u are independent and identically distributed according to a  $N[0, \sigma^2]$  distribution, where  $\sigma^2$  is an unknown constant, and k > 1. We wish to build a confidence interval with level 0.95 for the ratio  $\theta = \beta_2/\beta_1$ . Propose a method for doing this.
- (b) Suppose the elements of u are independent and identically distributed according to a σt(1) distribution, where t(1) represents a Student t distribution with 1 degree of freedom and σ is an unknown constant. Propose a method for testing the hypothesis H<sub>0</sub> : β<sub>1</sub> = 1 at level α = 0.05 in the context of this model such the size of the test is exactly equal to α = 0.05.

## References

DUFOUR, J.-M. (2006): "Monte Carlo Tests with Nuisance Parameters: A General Approach to Finite-Sample Inference and Nonstandard Asymptotics in Econometrics," *Journal of Econometrics*, 133(2), 443–477.