## ECONOMETRIC THEORY REVIEW QUESTIONS

## Multivariate dynamic models

- 1. Discuss the relationships between the following concepts:
  - (a) Granger causality and prediction;
  - (b) Granger causality and causality at several horizons;
  - (c) Granger causality and impulse response coefficients;
  - (d) causality at several horizons and impulse response coefficients.
- 2. Consider the process described by the following model:

$$X_t = \begin{bmatrix} X_{1t} \\ X_{2t} \end{bmatrix} = \begin{bmatrix} 1 - 0.5B & 0 \\ -0.5B & 1 - 0.2B \end{bmatrix} \begin{bmatrix} a_{1t} \\ a_{2t} \end{bmatrix}$$
 (1)

où  $t \in \mathbb{Z}$ ,  $a_t = [a_{1t}, a_{2t}]'$  is a sequence of *i.i.d.*  $N[0, \Sigma]$  random vectors with

$$\Sigma = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} . \tag{2}$$

- (a) What is the type of this process?
- (b) Is this process strictly stationary? Why?
- (c) Does this process have a Wold representation? If so, give it.
- (d) Is this process invertible? Why?
- (e) Does this process has an autoregressive representation? If so, give it.
- (f) Does the variable  $X_{2t}$  cause  $X_{1t}$  in the sense of Granger? Justify your answer.
- (g) Does the variable  $X_{1t}$  cause  $X_{2t}$  in the sense of Granger? Justify your answer.
- (h) Does the variable  $X_{2t}$  cause  $X_{1t}$  at all horizons? Justify your answer.
- (i) Does the variable  $X_{1t}$  cause  $X_{2t}$  at all horizons? Justify your answer.